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Mohammad Ashraf Asma Ali Vincenzo De Filippis *Editors* 

# Algebra and Related Topics with Applications

ICARTA-2019, Aligarh, India, December 17–19



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# Algebra and Related Topics with Applications

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*Editors* Mohammad Ashraf Department of Mathematics Aligarh Muslim University Aligarh, India

Vincenzo De Filippis Department of Engineering University of Messina Messina, Italy Asma Ali Department of Mathematics Aligarh Muslim University Aligarh, India

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### Preface

Algebra is considered a significant milestone in Mathematics. Algebra is not just limited to Mathematics; also, it has a lot of real-world applications be it computer science, chemical science, technology, coding theory, cryptography, graph theory, etc. In fact, the world revolves around the applications of algebra.

The Department of Mathematics, Aligarh Muslim University, Aligarh, India, organized an International Conference on Algebra and Related Topics with Applications (ICARTA-19) with the aim to provide a forum for researchers, eminent academicians, research scholars and students to exchange ideas, and to communicate and discuss research findings and new advances in different branches of algebra, especially Ring theory, Coding theory, Cryptography and Graph theory.

During the conference, world-renowned algebraists gave 8 plenary talks and 20 invited talks which have been potentially affected by the most recent developments in the related areas. This conference covered topics of several new directions and applications. Among the participants of the conference, 90 exuberant younger mathematicians presented their research articles, during proper thematic sessions. More than one dozen participants from various countries like USA, Egypt, Korea, Nigeria, Taiwan, Italy, Germany and Norway together with nearly two hundred delegates from within India participated in this conference.

A special session was devoted in the honour of Prof. M. A. Quadri who is one of the esteemed professors who initiated study and research in the area of modern mathematics in the Department of Mathematics, AMU, Aligarh.

We appreciate the active participation of all young researchers and academicians. Hopefully, the conference also enables participants to explore possible avenues to foster academic and research exchange, as well as scientific activities within and abroad of India. This refereed volume includes papers from renowned algebraists and invited speakers as well as other participants of the conference. All submitted papers are rigorously reviewed, followed by a careful selection process.

In addition to highlighting the latest research being done on the frontiers of algebra, the articles published also provide insights into how ideas have explored and have been connected. The proceeding's overall approach addresses the challenges of abundant topics of algebra particularly semi groups, groups, derivations in rings, rings and modules, group rings, matrix algebra, triangular algebra, polynomial rings and lattice theory. Apart from these topics, we also received research papers which have applications in coding theory and graph theory.

This research volume is distinguished from many others by its variety of topics, methodologies and depth of research. We believe that this volume will thus further expand our understanding and can serve as a reference book in the rapidly expanding field of algebra and related topics with their applications to coding theory, cryptography and graph theory.

We gratefully acknowledge the funding received towards this conference from the Aligarh Muslim University (AMU), Aligarh, Department of Science and Technology (DST), New Delhi, Indian National Science Academy (INSA), New Delhi, and the Council of Scientific and Industrial Research (CSIR), New Delhi. This volume would not have been possible without the support of expert referees who provided their valuable comments through reports diligently and promptly despite their busy schedules. We would like to thank Prof. M. Imdad, Chairman, Department of Mathematics, for his consistent support and guidance during the running of this conference. Furthermore, we would like to thank the rest of the faculty members, research scholars of Mathematics Department, AMU, for their collaborative effort during the conference. Also thanks to committee members, especially Prof. Nadeem ur Rehman, Dr. Shakir Ali, Dr. Mujeebur Rehman, Dr. M. Aslam Siddeeque and Dr. Ghulam Mohammad, who enabled this conference to be possible. We would like to say special thanks to Prof. M. A. Quadri. In spite of his health problems, his support, guidance and overall insights have made this an inspiring experience for us. We would like to express our gratitude to the entire team of Springer for publishing this volume. Thank you Mr. Shamim Ahmad, Senior Editor, Mathematical Sciences, Springer, India for facilitating the publication process, we truly appreciate your hard work and enthusiasm, everything was so intelligible and gave clear guidance. We look forward to continue our relationship.

Aligarh, India Aligarh, India Messina, Italy Mohammad Ashraf Asma Ali Vincenzo De Filippis

## Contents

#### Algebra

Characterization of <i>b</i> -generalized Derivations in Rings with Involution	3
Jordan Generalized <i>n</i> -derivations of Unital Algebras Containing Idempotents Mohd Shuaib Akhtar, Mohammad Afajal Ansari, and Nazia Parveen	11
Variational Analysis of Approximate Defective Eigenvalues	25
Structure of Prime Near Rings with Generalized Derivations Asma Ali and Inzamam ul Huque	39
<i>w</i> -FP-projective Modules and Dimensions Refat Abdelmawla Khaled Assaad, El Mehdi Bouba, and Mohammed Tamekkante	47
Central Values of X-generalized Skew Derivations on Right Ideals in Prime Rings Luisa Carini and Vincenzo De Filippis	59
<b>Commutative Polynomial Rings which are Principal Ideal Rings</b> Henry Chimal-Dzul	91
Two Remarks on Generalized Skew Derivations in Prime Rings Vincenzo De Filippis and Francesco Rania	101
Dimensional Dual Hyperovals—An Updated Survey Ulrich Dempwolff	115
A Note on FMS Modules and FCP Extensions Atul Gaur and Rahul Kumar	143

A Pair of Derivations of Prime Rings with Involution Shuliang Huang	149
Basic One-Sided Ideals of Leavitt Path Algebras over Commutative Rings	155
Pramod Kanwar, Meenu Khatkar, and R. K. Sharma	
<b>On Certain *-differential Identities in Prime Rings with Involution</b> Abdul Nadim Khan, Shakir Ali, Adnan Abbasi, and Mohammed Ayedh	167
On <i>b</i> -Generalized Derivations in Prime Rings Mohammad Salahuddin Khan	181
Commutativity of *-Prime Rings with Generalized Derivations on *-Jordan Ideals	191
Deepak Kumar and Bharat Bhushan	
<b>Local Subsemigroups and Variants of Some Classes of Semigroups</b> Siji Michael and P. G. Romeo	207
Closed Weak Supplemented Lattices	217
<b>On Compatible Ring Structures of the Injective Hull of a Ring</b> Jae Keol Park and S. Tariq Rizvi	227
On Commutators Involving Derivations and Automorphisms in Prime Rings	263
Mohd Arif Raza, Mohammad Shadab Khan, and Nadeem ur Rehman	
Modules Invariant Under Clean Endomorphisms of Their Injective Hulls	269
Jane Roseline and Manoj Kumar Patel	
A Note on Central Idempotents in Finite Group Rings of Symmetric	777
Groups Anuradha Sabharwal, Pooja Yadav, and R. K. Sharma	211
Jordan Product Preserving Generalized Skew Derivations on Lie Ideals	287
Giovanni Scudo	
Prime Rings with Generalized Derivations and Power Values on Lie Ideals	211
Mohammad Aslam Siddeeque, Ali Ahmed Abdullah, and Nazim Khan	311
Coding Theory	
On the Purity of Resolutions of Stanley-Reisner Rings Associated to Reed-Muller Codes	325
Sudhir R. Ghorpade and Rati Ludhani	

Contents

Skew Constacyclic Codes over $F_q + vF_q$ Ghulam Mohammad, Naim Khan, and Almas Khan	337
<b>Cyclic and LCD Codes over a Finite Commutative Semi-local Ring</b> Om Prakash, Habibul Islam, and Arindam Ghosh	349
Graph Theory	
Some Recent Results on the Graphs of Finite-Dimensional Vector Spaces	363
Two Value Graph Magma Algebras and AmenabilityPınar Aydoğdu, Joaquín Díaz Boils, Sergio R. López-Permouth,and Rebin A. Muhammad	383
Graph of Linear Transformations Over $\mathbb{R}$ Ayman Badawi and Yasmine El-Ashi	401
On Distance Laplacian (Signless) Eigenvalues of Commuting Graphs of Dihedral and Dicyclic Groups S. Pirzada, Bilal A. Rather, Rezwan ul Shaban, and Imran Bhat	413
Spectrum of Graphs over Rings: A Survey V. Rabikka, T. Asir, and M. Evangeline Prathibha	427
On a New Extension of Annihilating-Ideal Graph of Commutative Rings	451
Spectrum of the 3-zero-divisor Hypergraph of Some Classes of Local Rings K. Selvakumar, J. Beautlin Jemi, and Nadeem ur Rehman	463
Complement of the Generalized Total Graph of Commutative         Rings – A Survey         T. Tamizh Chelvam	477

xiii