Lecture Notes in Mathematics 2308
CIMF Foundation Subseries

Massimo Chiappini Vincenzo Vespri *Editors* 

# Applied Mathematical Problems in Geophysics

Cetraro, Italy 2019





# Lecture Notes in Mathematics

# C.L.M.E. Foundation Subseries

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Massimo Chiappini • Vincenzo Vespri Editors

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