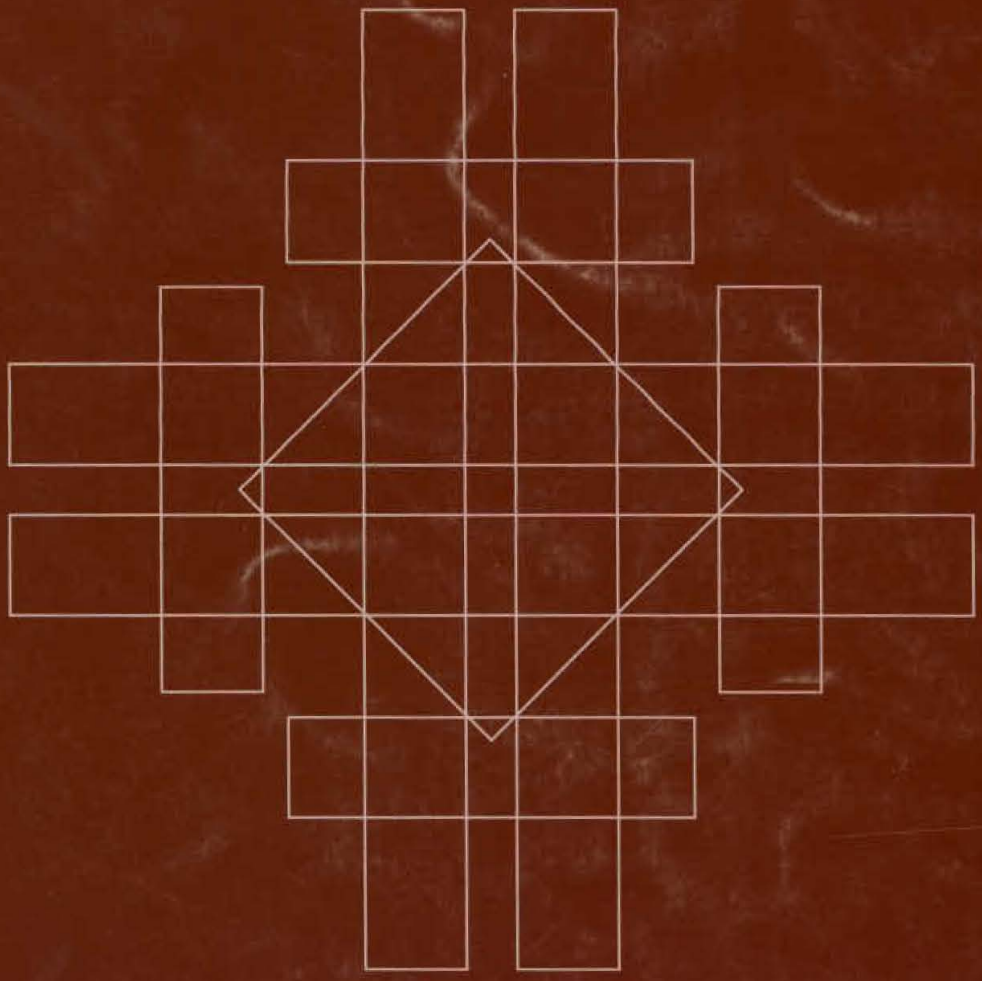
PROCEEDINGS OF THE TWENTY-SIXTH ANNUAL SYMPOSIUM ON

COMPUTATIONAL GEOMETRY

(SCG'10)



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