D. Dolev Z. Galil M. Rodeh (Eds.)

# Theory of Computing and Systems

ISTCS '92, Israel Symposium Haifa, Israel, May 27-28, 1992 Proceedings

. Cc 01-602

•

### Springer-Verlag

Berlin Heidelberg New York London Paris Tokyo Hong Kong Barcelona Budapest Series Editors

Gerhard Goos Universität Karlsruhe Postfach 6980 Vincenz-Priessnitz-Straße 3 W-7500 Karlsruhe, FRG Juris Hartmanis Department of Computer Science Cornell University 5149 Upson Hall Ithaca, NY 14853, USA

Volume Editors

Danny Dolev Hebrew University Givat Ram, Jerusalem, Israel

Zvi Galil Columbia University, New York, NY 10027, USA and Tel Aviv University Ramat Aviv, Tel Aviv, Israel

Michael Rodch IBM Israel Utd., Science and Technology, Technion City Haifa 32000, Israel

CR Subject Classification (1991): F.1-4, B.3, C.2, G.1-2, I.1, E.4, D.2-3

ISBN 3-540-55553-6 Springer-Verlag Berlin Heidelberg New York ISBN 0-387-55553-6 Springer-Verlag New York Berlin Heidelberg

This work is subject to copyright. All rights are reserved, whether the whole or part of the material is concerned, specifically the rights of translation, reprinting, re-use of illustrations, recitation, broadcasting, reproduction on microfilms or in any other way, and storage in data banks. Duplication of this publication or parts thereof is permitted only under the provisions of the German Copyright Law of September 9, 1965, in its current version, and permission for use must always be obtained from Springer-Verlag. Violations are liable for prosecution under the German Copyright Law.

© Springer-Verlag Berlin Heidelberg 1992 Printed in Germany

6223

Typesetting: Camera ready by author/editor Printing and binding: Druckhaus Beltz, Hemsbach/Bergstr. 45/3140-543210 - Printed on acid-free paper

## Foreword

ISTCS'92 — The Israel Symposium on the Theory of Computing and Systems, came about spontaneously as a result of informal interaction between a group of people who viewed the conference as an appropriate expression of Israeli strength in theoretical aspects of computing and systems. These people then created the following organizational structure:

#### Symposium Chairs

Zvi Galil, Columbia and Tel-Aviv U. Michael Rodeh, IBM Israel

#### Program Committee

Catriel Beeri, Hebrew U.Shmuel Katz, TechnionDanny Dolev (Chair), Hebrew U.Nimrod Megiddo, IBM Almaden Research CenterNissim Francez, TechnionYoram Moses, Weizmann InstituteShafi Goldwasser, MITEhud Shapiro, Weizmann InstituteAlon Itai, TechnionAmiram Yehudai, Tel Aviv U.

#### Local Arrangements

Shmuel Katz, Technion

The enthusiasm that the symposium created took three major forms: submission of high quality papers which led to strict acceptance criteria; acceptance of the symposium invitation to deliver an invited talk by Richard M. Karp and Michael O. Rabin, and positive response to requests for sponsorship/cooperation by non-profit professional organizations, computer-related industrial organizations, and academic institutions:

Sponsorship. The Israel Academy of Sciences and Humanities, Israel Association of Electronic Industries, the Leibniz Center for Research in Computer Science, the Hebrew University of Jerusalem, and U.S. National Science Foundation.

Cooperation. The ACM Special Interest Group for Automata and Computability Theory (SIGACT), IEEE Computer Society, IEEE Israeli Chapter, and ILA -Information Processing Association of Israel.

Industrial Sponsors. Digital (Israel) Ltd., IBM (Israel) Ltd., Intel Ltd., Motorola Communications Ltd., and National Semiconductors. We thank all the organizations that have helped make this symposium successful. Thanks are also due to the Technion for helping in organizing the symposium, and to Springer Verlag, Heidelberg, for accepting the task of getting this volume into press in a very brief time interval.

April 1992

Danny Dolev Zvi Galil Michael Rodeh

This article was processed using the BTEX macro package with LLNCS style

# Table of Contents

Merging and Splitting Priority Queues and Deques in Parallel Jingsen Chen	1
Lower Bounds for the Complexity of Functions in a Realistic RAM Model Nader H. Bshouty	12
On Boolean Decision Trees with Faulty Nodes	24
Interval Graphs, Interval Orders and the Consistency of Temporal Events Martin Charles Golumbic, Ron Shamir	32
Higher Order Functions in First Order Theory	43
Reduction Relations in Strict Applicative Languages	55
Approximation Algorithms for Minimum Time Broadcast	67
The Complexity of Reconfiguring Network Models	79
Optimal Mapping in Direct Mapped Cache Environments	91
New Algorithms for Generalized Network Flows	103
Factoring Polynomials via Relation-Finding	115
New Resultant Inequalities and Complex Polynomial Factorization Victor Pan	122
Can Symmetric Toeplitz Solvers be Strongly Stable?	137
Bounds On Parallel Computation of Multivariate Polynomials	147
Time-Lapse Snapshots	154

Concurrent Timestamping Made Simple	171
Distributed Evaluation: A Tool for Constructing Distributed Detection Programs	184
Foundations of Asymptotical Theory of Determinate Compact Testing	195
Optimal K-Colouring and K-Nesting of Intervals	207

This article was processed using the  $\ensuremath{\mathbb{B}}\ensuremath{\mathrm{T}}_EX$  macro package with LLNCS style

# Merging and Splitting Priority Queues and Deques in Parallel

Jingsen Chen

Department of Computer Science, Lund University, Box 118, S-221 00 Lund, Sweden

Abstract. We investigate the parallel complexity of merging priority queues and double-ended priority queues (priority deques, for short). The implicit data structures that implement the queues studied in this paper are the heap, the twin-heap, the min-max heap, and the deap. It is known that heaps can be merged sequentially in sublinear time whereas merging min-max heaps requires linear sequential time. In this paper, we design efficient  $O(\log n)$ time parallel algorithms to merge two priority queue or deque structures of the same type on n and k elements  $(n \ge k)$ , respectively, which achieves the optimal speed-up. More precisely, two heaps of sizes n and k can be merged in  $O(\log n)$  time with log k processors. Moreover, a related problem of splitting a heap on n elements into two heaps of sizes k and n - k is solved in  $O(\log n)$  parallel time with  $\log n$  processors, which also achieves the optimal speed-up. For the merge operation on priority deques, we show that the problem of merging twin-heaps can be solved in the same complexity as that for heaps both sequential and in parallel. Algorithms for merging two min-max heaps or two deaps of sizes n and k are demonstrated, which achieves a parallel time of  $O(\log n)$  with  $\frac{k}{\log n} + \log k$  processors. The study of parallel solution to the problem of merging deaps also provides us with the first serial deap merging algorithm of time complexity  $O(k + \log n \cdot \log k)$ . The parallel computation model used in this paper is the EREW PRAM (Exclusive-Read Exclusive-Write Parallel Random Access Machine).

#### 1 Introduction

One of the fundamental data types in computer science is the priority queue. It has been useful in many applications [1, 14]. A *priority queue* is a set of elements on which two basic operations are defined: insert a new element into the set; and retrieve and delete the minimum element of the set. Several data structures have been proposed for implementing priority queues. The probably most elegant one is the heap, which was introduced by Williams [21].

The problems of constructing, merging, and splitting heaps have received considerable attention in the literature [7, 10, 11, 12, 14, 15, 19, 20] and sequential constructing algorithms of linear time and sublinear time heap merging and splitting algorithms have been developed. However, designing optimal heap construction and heap merging and splitting algorithms in parallel models of computation has not been so deeply studied. Recently, Rao and Zhang [18] presented a  $\Theta(\log n)$  worst case time EREW parallel algorithm for building a heap on n elements and Carlsson and Chen [6] reduced the time for the construction to  $\Theta((\log \log n)^2)$  on the parallel comparison tree model.