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VDM '90 VDM and Z – Formal Methods in Software Development

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Foreword

The present volume is the third in a series of VDM Symposia Proceedings. The previous two VDM Symposia were held in March 1987 in Brussels, Belgium, and in September 1988 in Dublin, Ireland. Their proceedings were published by Springer-Verlag in the same series as this volume, as Lecture Notes in Computer Science volumes 252 ([1]) and 328 ([2]), respectively.

VDM and Z are acronyms. VDM stands for Vienna Development Method, while Z refers to Zermelo, a fine mathematician whose name is associated with set theory. VDM arose out of an industrial project at the IBM Vienna Laboratory in the early 1970s. Z was first masterminded by J.-R. Abrial, who laid down the basic ideas while at Oxford in the very early 1980s. VDM later moved into academia, lacking industrial support at first, while Z had the good fortune of getting industrial support.

The preface by Tony Hoare gives an interesting view of the uniting and distinct features of VDM and Z.

The Commission of the European Communities (CEC) has had the fortunate vision to form, around 1985, VDM Europe, which is a group of industrial and academic software engineers, programmers and scientists interested in model-theoretic formal software development methods. VDM Europe advises the CEC. VDM Europe is partially supported by the CEC and meets in Brussels 3–4 times yearly to discuss practical, technical and scientific matters. These are: industrial experience and applications, tools, college and university education and industry training, specification and design methodology and techniques, formalisation and formal foundations, and standardisation. The British Standards Institute (BSI) is currently formulating a standard for the VDM Specification Language (SL) — a standard that will also be proposed to the ISO. That standard will contain fully formal, mathematical definitions of the semantics of the BSI VDM SL.

In the UK there is a group similar to VDM Europe called the Z Users Group.

While planning this symposium VDM Europe felt it reasonable, given the commonalities outlined in Tony Hoare's preface, to invite the Z community to join that of VDM in presenting our achievements.

Many computing science, programming and software engineering proceedings are published regularly. The ones by VDM Europe have the distinguishing mark, we believe, that they are concerned with bringing real theory to apply to real programming. This is true both for VDM and Z. In the proceedings of the VDM Symposia you will therefore find a refreshing blend of papers from industry and from academia. In fact you will witness an enjoyable cross fertilisation and co-operation between the two sides.

In Europe we are very much interested in methodology, semantics and techniques, that is, in understanding how we build and what it is that we are building.

Thus, non-European readers will find a somewhat biased selection of papers in these proceedings.

The papers in these proceedings basically fall into four major groups: Applications, Methodology, Formalisations, and Foundations. The Methodology group has been further subdivided into five areas: Specification Methodology, Design Methodology, Modularity, Object Orientedness, and Processes, Concurrency and Distributed Systems. Obviously the borderlines between these are fuzzy. We have chosen to present Applications first, and Foundations last. We wish the casual reader from industry to adopt the message of VDM and Z, namely apply formal, model-theoretic techniques in order to have fun, to achieve correct software, etc. Therefore we open with what is closest to the needs of industry by showing that indeed real applications can be formalised, and to great advantage. This is in contrast to an academic style of presentation which, after the fact, would normally present foundations first!

By a method we mean a set of procedures, used by humans, in selecting and applying techniques and tools in order to efficiently achieve the construction of efficient artifacts — here programs and software. By a formal method we mean one which permits mechanical support of rigorous development, that is, rigorous reasoning aided by mechanical type checking, semantic analysis, specification to design transformation, animation, proof assistance, verification and even theorem proving. Our sub-division into areas reflects techniques, albeit overlapping ones.

The Formalisation group has been sub-divided into Formalisation (!) and Type Systems. By formalisation we mean explaining formal systems, such as VDM and Z, in terms of some (other) formal specification system, including mathematics. By foundation we mean (examination of) the means in terms of which we explain. Type systems deal with a properly contained area of formalisation (and its 'mechanisation').

The invited papers were selected to reflect openness towards ideas that may not necessarily have arisen in the context of model-theoretic software development. Previous VDM Symposia featured presentations by Don Good: *Computing is a Physical Science*, and J.-R. Abrial: *The B Tool*. We are very fortunate, at this Symposium, to have three similarly exciting presentations: Ole-Johan Dahl: *Object Orientation and Formal Techniques*, Joseph A. Goguen: *Algebraic Approaches to Refinement* and Reiichi Nakajima: *Modal Logic Programming*. We thank these invited speakers for their kind willingness to serve.

References

- [1] *VDM'87: VDM — A Formal Method at Work* (Eds. D. Bjørner, C. B. Jones, M. Mac an Airchinnigh and E. J. Neuhold) Proceedings, VDM-Europe Symposium 1987, Brussels, Belgium, March 1987, Springer-Verlag, Lecture Notes in Computer Science, vol. 252, IX + 422 pages, 1987.
- [2] *VDM'88: VDM — The Way Ahead* (Eds. R. Bloomfield, L. Marshall and R. Jones) Proceedings, 2nd VDM-Europe Symposium 1988, Dublin, Ireland, September 1988, Springer-Verlag, Lecture Notes in Computer Science, vol. 328, IX + 499 pages, 1988.

Preface

C.A.R. Hoare

I am delighted to be asked to welcome you to this international conference on VDM and Z. Your programme committee and organisers have worked hard to ensure that you will enjoy the occasion and benefit from it by increased understanding and confidence in the use of new methods in software engineering. My particular delight is that this conference, by its title and its content, is a welcome rapprochement between two technically sound and practically successful mathematical approaches to the specification and design of software.

The reason for their success is the same. Both VDM and Z insist that the specification of requirements should be formulated from the beginning at the highest possible level of abstraction, using all the available power of mathematics to describe the desirable, observable and testable properties of the product which is to be implemented. An abstract specification leaves greatest scope for exercise of ingenuity and judgement to meet targets of cost and efficiency in the subsequent design and implementation of the product; and correctness can be assured by observance of certain engineering procedures, which are soundly based on mathematical calculations.

VDM and Z share a common philosophy and a common method; but to many sympathetic supporters and potential users it seems both sad and strange that they seem to have different styles and notations, and to have given rise to disunity and disagreement among two apparently distinct schools of thought. The less sympathetic observer might be reminded of theological disputations of the Middle Ages leading to schisms, inquisitions and wars. How did such a situation arise? Was it due to historical, political or commercial accident? Or even to ignorance, incompetence or personal pride? Since I have been an actor in the history from the early days, I must acknowledge my share of the blame, if blame there be.

VDM, as its name implies, was originally designed as a method for sound development of concrete data structures from abstract specifications. It was based on proof of a commuting property like that of homomorphisms in algebra or natural transformations in category theory. Its designers were familiar with the important role of functions in mathematics, and the charming way in which they can be defined by recursion. They had an early and extensive experience of the use of formal methods in the specification, design and implementations of programming languages. These factors had an influence on the style and content of early versions of VDM.

The designers of Z started with the confidence provided by VDM that highly abstract specifications can be reliably implemented as programs. The design team were therefore able to concentrate attention on the earlier phases of requirements

capture and system-wide specification. J.-R. Abrial had a prior interest in the axiomatic foundations of mathematics, including the theory of sets and relations. At Oxford, we were also familiar with Dijkstra's predicate-based calculus of procedural programming, including non-determinism. This explains the slightly different emphasis placed on different branches of mathematics by VDM and Z.

Finally, at Oxford we were fortunate in obtaining an industrial sponsor interested primarily in improving the specification phase of the design of a large software product, and willing to postpone consideration of formal design and implementation. But the advantage of building on the success of VDM has also a sharp edge; the only point of the research was to suggest improvements and advances on what was already known and practised. And that was indeed a significant challenge, because the ultimate goal is that the designers and users of VDM would adapt and adopt the more successful technical and stylistic improvements suggested by our research. This has already happened: the mutual beneficial influence of Z and VDM is now so great that many of my remarks are of purely historical significance.

One of the first discoveries of the research by the Z team was the necessity of separating small chunks of formal material by paragraphs of informal prose, explaining the relationship between the formal symbols and reality, and motivating the decisions that are captured by the formalisation. The drafting of the informal prose was even more difficult to teach, learn and practice than the mastery of mathematical notations and concepts. But the need to simplify interleaving of formal and informal material led inevitably to the Z schema, with its free variables declared as its signature, and even to the box convention introduced to separate formula from text.

The next requirement is for modularity: it must be possible to formalise individual requirements separately, and join them together by simple connectives with obvious meanings. The simplest, most obvious and most necessary connective is conjunction: we want the product to meet this requirement *and* that requirement. We also need the kind of abstraction that can be achieved by disjunction: we want the product to have this property *or* that one, but the decision can be postponed perhaps even to the implementation. And a third propositional operator, negation, is useful in placing overall constraints on the behaviour of the product, for example to achieve safety. The schema calculus of Z is based on these simple propositional connectives.

Finally, we need to start our specifications with a simple description of the general structure of the system, with as few variables, parameters and operations as possible; and then leave this original text unchanged while later adding more detail. This can be achieved by embedding the initial general schema inside its particular extensions, thereby achieving a hierarchy like that exploited in object oriented programming.

That is my explanation of the early distinctive features of the Z schema calculus. Each one of them was subjected at the time to rigorous discussion and

evaluation, and only the most essential have survived. All of them arise almost inevitably from the need to simplify and clarify specifications. However, they are completely irrelevant in the design and development phase of system implementation, for which the notations, concepts and methods of VDM are designedly more appropriate. So the obvious advice to the practitioner is to use each notation for its primary intended purpose: Z for specification and VDM for development. Of course the transition between these two phases involves a translation, in which the separate schemas of the Z specification are assembled, and the VDM preconditions are calculated and checked. But such calculations are in any case essential to check the completeness and consistency of the specification; they are not just due to fortuitous notational incompatibility. Similar checks and changes of style and notation abound in all mature engineering disciplines. No one now specifies a computer architecture using only boolean algebra, but no computer can be designed without it.

So why was this obvious reconciliation of the complementary merits of Z and VDM not recognised earlier and more widely? The reason is equally obvious - it is scientifically inelegant and in practice very wasteful to use two notations if there is any conceivable chance that a single notation will do the whole job. So intensive research is required to see if either of the two notations can be used, extended or adapted for both purposes. And it is entirely reasonable to engage more than one team of scientists on this important task, and that each team should choose a different starting point, and that they should work in a spirit of friendly rivalry. But as scientists, everyone must have a deep respect for the merits and achievements of the rival team, and strong desire to learn from them. Preservation of scientific objectivity must be an overriding concern. The same goal is pursued by all, namely, the advancement of knowledge to a point at which we can give obvious and definitive answers to the basic questions.

1. Is one notation (or the other, or both) adequate for both specification and development?
2. If distinct notations are desirable, can this be justified by appeal to general scientific, mathematical or engineering principles?
3. In the latter case, what measures are recommended for easy and reliable transition between notations?

There are many software engineers and their managers who believe or hope that a single notation should be used not only for specification and development but also for prototyping and even production programming. Many millions of dollars have been expended in the search for such a notation and its implementation. But experience of other branches of mathematics and engineering suggests strongly that no uniform notation can be adequate for all purposes. And in the case of programming, we know both in theory and in practice that abstract notations appropriate

for specification are either incomputable or would take super-astronomical time to execute, even as prototypes.

In the light of recent excellent research, by teams concentrating on each of the two notations, I am now inclined to believe that there are certain fundamental differences between the structuring principles appropriate to specification and to development; and that we should begin to turn our attention to collaboration, in seeking the answers to question 2 and 3, which will ease the transition between these two essential phases of software engineering.

That is why this conference on VDM and Z is so welcome and so timely. It provides a forum at which we can exchange our understandings and experiences as an essential prelude to faster scientific progress. It also sends a signal to the potential users of formal methods that we recognise a common scientific method and a common goal - which is to give them the best possible assistance in their ever more difficult task of programming computers reliably to meet their genuine needs. When we have achieved that together, we will not care by what name the method is called, or whether the formulae are enclosed in boxes.

We are not engaged in theological wrangling, let alone religious war. There is no need for a potential user to delay introduction of formal methods until "the experts" have resolved their differences. It is possible even now to gain experience and benefit from any formal method soundly based in mathematics, and to extend the method gradually into all phases of the software lifecycle, taking advantage of new developments and discoveries as they emerge from our research.

That is the message of the title of this conference. I hope that the spirit of that message will permeate the conference, and remain with us when we leave.

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This symposium would not have been possible without the voluntary and dedicated work by all of the PC members:

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The PC Chairman thanks all and everybody for their patience and forbearance with their chairman.

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We are sure that all participants at the symposium will rightfully appreciate the hard work this committee has laid down in order to secure a successful symposium.

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All submitted papers — whether accepted or rejected — were refereed by the programme committee (PC) members. Most papers were, in addition, refereed by colleagues.

All papers were refereed by at least three reviewers.

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The Programme Committee extends its grateful thanks to the very thorough job done by all referees.

We apologize if, inadvertently, we have omitted a non-PC referee from the above list. To the best of our knowledge the above is accurate.

Sponsors

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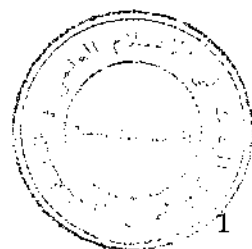
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