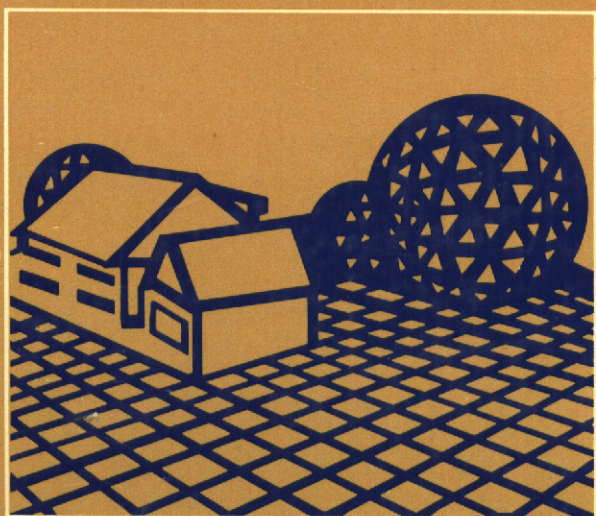


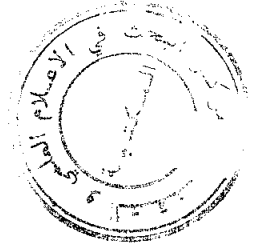
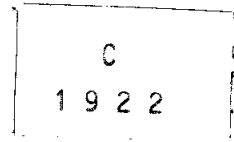
COMPUTER VISION

DANA H. BALLARD • CHRISTOPHER M. BROWN



COMPUTER VISION

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