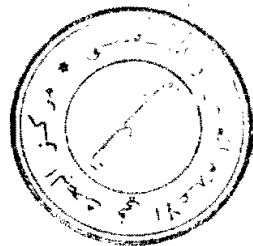


DISTRIBUTED ALGORITHMS FOR ELECTION IN UNIDIRECTIONAL AND COMPLETE NETWORKS

Yehuda Afek

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Los Angeles

Distributed Algorithms for Election in
Unidirectional and Complete Networks

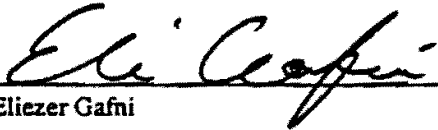
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in Computer Science

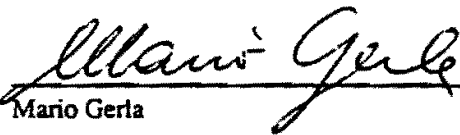
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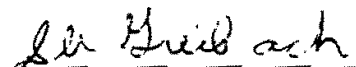
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