

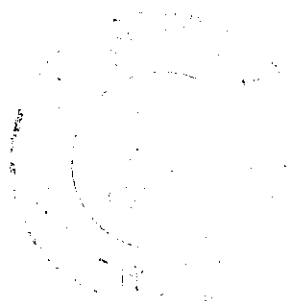
Hans Delfs
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Introduction to Cryptography

Principles and Applications



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Hans Delfs • Helmut Knebl

Introduction to Cryptography

Principles and Applications



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Preface

The rapid growth of electronic communication means that issues in information security are of increasing practical importance. Messages exchanged over worldwide publicly accessible computer networks must be kept confidential and protected against manipulation. Electronic business requires digital signatures that are valid in law, and secure payment protocols. Modern cryptography provides solutions to all these problems.

This book originates from courses given for students in computer science at the Georg-Simon-Ohm University of Applied Sciences, Nürnberg. It is intended as a course on cryptography for advanced undergraduate and graduate students in computer science, mathematics and electrical engineering.

In its first part (Chapters 1–4), it covers - at an undergraduate level - the key concepts from symmetric and asymmetric encryption, digital signatures and cryptographic protocols, including, for example, identification schemes, electronic elections and digital cash. The focus is on asymmetric cryptography and the underlying modular algebra. Since we avoid probability theory in the first part, we necessarily have to work with informal definitions of, for example, one-way functions and collision-resistant hash functions.

It is the goal of the second part (Chapters 5–10) to show, using probability theory, how basic notions like the security of cryptographic schemes and the one-way property of functions can be made precise, and which assumptions guarantee the security of public-key cryptographic schemes such as RSA. More advanced topics, like the bit security of one-way functions, computationally perfect pseudorandom generators and the close relation between the randomness and security of cryptographic schemes, are addressed. Typical examples of provably secure encryption and signature schemes and their security proofs are given.

Though particular attention is given to the mathematical foundations and, in the second part, precise definitions, no special background in mathematics is presumed. An introductory course typically taught for beginning students in mathematics and computer science is sufficient. The reader should be familiar with the elementary notions of algebra, such as groups, rings and fields, and, in the second part, with the basics of probability theory. Appendix A contains an exposition of the results from algebra and number theory necessary for an understanding of the cryptographic methods. It includes proofs

and covers, for example, basics like Euclid's algorithm and the Chinese Remainder Theorem, but also more advanced material like Legendre and Jacobi symbols and probabilistic prime number tests. The concepts and results from probability and information theory, which are applied in the second part of the book, are given in full in Appendix B. To keep the mathematics easy, we do not address elliptic curve cryptography. We illustrate the key concepts of public-key cryptography by the classical examples like RSA in the quotient rings \mathbb{Z}_n of the integers \mathbb{Z} .

The book starts with an introduction into classical symmetric encryption in Chapter 2. The principles of public-key cryptography and their use for encryption and digital signatures are discussed in detail in Chapter 3. The famous and widely used RSA, ElGamal's methods and the digital signature standard, Rabin's encryption and signature schemes serve as the outstanding examples. The underlying one-way functions – modular exponentiation, modular powers and modular squaring – are used throughout the book, also in the second part.

Chapter 4 presents typical cryptographic protocols, including key exchange, identification and commitment schemes, electronic cash and electronic elections.

The following chapters focus on a precise definition of the key concepts and the security of public-key cryptography. Attacks are modeled by probabilistic polynomial algorithms (Chapter 5). One-way functions as the basic building blocks and the security assumptions underlying modern public-key cryptography are studied in Chapter 6. In particular, the bit security of the RSA function, the discrete logarithm and the Rabin function is analyzed in detail (Chapter 7). The close relation between one-way functions and computationally perfect pseudorandom generators meeting the needs of cryptography is explained in Chapter 8. Provable security properties of encryption schemes are the central topic of Chapter 9. It is clarified that randomness is the key to security. We start with the classical notions of provable security originating from Shannon's work on information theory. Typical examples of more recent results on the security of public-key encryption schemes are given, taking into account the computational complexity of attacking algorithms. A short introduction to cryptosystems, whose security can be proven by information-theoretic methods without any assumptions on the hardness of computational problems ("unconditional security approach"), supplements the section. Finally, we discuss in Chapter 10 the levels of security of digital signatures and give examples of signature schemes, whose security can be proven solely under standard assumptions like the factoring assumption, including a typical security proof.

Each chapter (except Chapter 1) closes with a collection of exercises. Answers to the exercises are provided on the Web page for this book: www.informatik.fh-nuernberg.de/DelfsKnebl/Cryptography.

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Nürnberg, December 2001

Hans Delfs, Helmut Knebl

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