

ARTIFICIAL INTELLIGENCE SERIES

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Logic for Problem Solving

Robert Kowalski

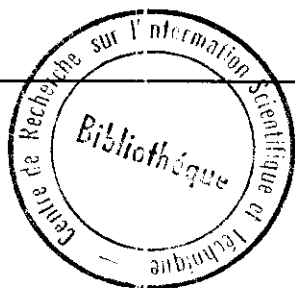


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Logic for Problem Solving

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NORTH-HOLLAND

NEW YORK • AMSTERDAM • OXFORD

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Table of Contents

1	Introduction.....	1
	The family relationships example and clausal form.....	2
	A more precise definition of clausal form.....	5
	Top-down and bottom-up presentation of definitions.....	7
	Semantics of clausal form.....	8
	The fallible Greek example.....	10
	The factorial example.....	10
	The universe of discourse and interpretations.....	12
	A more precise definition of inconsistency.....	14
	The semantics of alternative conclusions.....	16
	Horn clauses.....	16
	Mushrooms and toadstools.....	17
	Exercises.....	18
2	Representation in Clausal Form.....	22
	Infix notation.....	22
	Variables and types of individuals.....	23
	Existence.....	25
	Negation.....	28
	Denial of conclusions which are implications.....	28
	Conditions which are implications.....	29
	Definitions and "if-and-only-if".....	31
	Semantic networks.....	31
	Extended semantic networks.....	33
	The representation of information by binary predicate symbols.....	33
	Advantages of the binary representation.....	36
	Databases.....	37
	Data query languages.....	39
	Data description.....	39
	Integrity constraints.....	40
	A departmental database.....	41
	Equality.....	42
	Exercises.....	44
3	Top-down and Bottom-up Horn Clause Proof Procedures.....	49
	Introduction.....	49
	The parsing problem.....	49
	A predicate logic representation of the parsing problem.....	52
	Bottom-up inference.....	53
	Top-down inference.....	55
	The family relationships example.....	57
	Inference rules and search strategies.....	60
	Infinite search spaces: natural numbers.....	64
	Definitions.....	67
	Substitution and matching.....	70
	Correctness and completeness of inference systems.....	71
	Exercises.....	71
4	Horn Clause Problem-Solving.....	75
	Path-finding.....	75
	The water containers problem.....	75
	A simplified path-finding problem.....	77
	Graph-representation of search spaces.....	79

Table of Contents

The Search Spaces for the Water Containers Problem.....	81
Search strategies for path-finding.....	83
The and-or tree representation of problem-reduction.....	85
The problem-solving interpretation of Horn clauses.....	88
Splitting and independent subgoals.....	89
Dependent subgoals.....	91
Finding versus showing.....	92
Lemmas, duplicate subgoals and loops.....	94
Search strategies for problem-reduction spaces.....	95
Bi-directional problem-solving.....	99
A notation for describing bi-directional problem-solving.....	101
Another formulation of the path-finding problem.....	102
Other aspects of problem-solving.....	103
Exercises.....	104
 5 The Procedural Interpretation of Horn Clauses.....	 107
Terms as data structures.....	107
Computation by successive approximation to output.....	109
The variation of input-output parameters.....	110
Non-determinism ₁ : several procedures match a procedure call.....	111
Sequential search regarded as iteration.....	112
"Don't know" versus "don't care" non-determinism.....	113
Non-determinism ₂ : The scheduling of procedure calls.....	114
Bottom-up execution of programs.....	118
The pragmatic content of logic programs.....	120
Separation of data structures.....	121
Terms versus relations as data structures.....	122
Database formalisms and programming languages.....	124
Algorithm = Logic + Control.....	125
Specification of the control component.....	127
Natural Language = Logic + Control.....	129
Exercises.....	129
 6 Plan-Formation and the Frame Problem.....	 133
Plan-formation and the blocks world.....	133
A clausal representation of the blocks world problem.....	134
Bottom-up execution of the state space axiom (12).....	138
Bottom-up execution of the frame axiom (15).....	139
Mixed top-down and bottom-up execution of the frame axiom.....	140
Top-down execution of the state space and frame axioms.....	143
Applications of plan-formation.....	144
Limitations.....	145
Exercises.....	146
 7 Resolution.....	 147
Negative goals and assertions.....	147
Resolution.....	149
Middle out reasoning with Horn clauses.....	150
Propositional logic example.....	151
Arrow notation for non-Horn clauses.....	156
Disjunctive solutions to non-Horn clause problems.....	157
Factoring.....	159
Exercises.....	160

Table of Contents

8 The Connection Graph Proof Procedure.....	163
The initial connection graph.....	163
The Resolution of links in connection graphs.....	165
Mixed top-down and bottom-up search - the parsing problem.....	168
Macro-processing and middle-out reasoning.....	169
Arrow notation for controlling selection of links.....	170
Self-resolving clauses.....	173
Deletion of links whose resolvents are tautologies.....	174
The connection graph proof procedure.....	175
Exercises.....	177
9 Global Problem-Solving Strategies.....	179
Deletion of redundant subgoals.....	180
Addition of surrogate subgoals.....	181
Rejection of inconsistent goal statements.....	182
Generalising the use of diagrams in geometry.....	183
Goals as generalised solutions.....	184
Goal transformation and the information explosion.....	185
Loop detection by analysis of differences.....	185
The factorial example.....	187
Invariant properties of procedures.....	188
Exercises.....	190
10 Comparison of Clausal Form with Standard Form.....	193
Introduction to the standard form of logic.....	193
Conversion to clausal form.....	197
Comparison of clausal form with standard form.....	200
Conjunctive conclusions and disjunctive conditions.....	200
Disjunctive conclusions.....	202
Only-if halves of definitions.....	202
Implications as conditions of implications.....	202
Derivation of programs from specifications.....	204
Exercises.....	206
11 If-and-only-if.....	210
The need for the only-if halves of definitions.....	211
Terms versus relations as data structures.....	212
The unstated only-if-assumption.....	213
Ambiguity of only-if.....	215
Object language and meta-language solutions.....	215
Object language and meta-language interpretations of negation.....	217
Horn clauses augmented with negation interpreted as failure.....	219
Proof of program properties.....	221
The monotonicity criticism of logical consequence.....	222
Exercises.....	223
12 Formalisation of Provability.....	225
Correct representability.....	226
A simple definition of a provability relation.....	227
Direct execution versus simulation.....	228
Addition and suppression of assumptions.....	230
Bootstrapping.....	231

Table of Contents

Combining the object language and meta-language.....	232
Incompleteness of the combined object and meta-language.....	233
More comprehensive form of the Demonstrate relation.....	234
Exercises.....	235
13 Logic, Change and Contradiction.....	239
Information systems.....	239
Dynamics of information system change.....	240
Restoration of consistency.....	242
A logic program for natural language.....	244
Conclusion.....	246
References.....	247
Index.....	261