

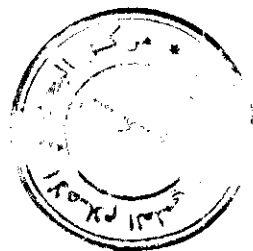
BIBLIOTHEQUE DU CERIST

NICKLAUS WIRTH

Algorithms +
Data
Structures =
Programs

PRENTICE-HALL
SERIES IN
AUTOMATIC
COMPUTATION

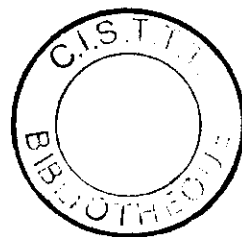
BIBLIOTHEQUE DU CERIST



ALGORITHMS + DATA STRUCTURES = PROGRAMS

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